

## Formulaire lié à la transformation en Z

| Signal causal<br>$n \mapsto x(n)$ pour $n \in \mathbb{N}$                                  | Transformée en Z<br>$z \mapsto (Zx)(z)$  |
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| $e(n) = 1$   | $(Ze)(z) = \frac{z}{z - 1}$  |
| $\begin{cases} d(0) = 1 \\ d(n) = 0 \text{ si } n \neq 0 \end{cases}$                      | $(Zd)(z) = 1$  |
| $r(n) = n$   | $(Zr)(z) = \frac{z}{(z - 1)^2}$  |
| $c(n) = n^2$   | $(Zc)(z) = \frac{z(z + 1)}{(z - 1)^3}$   |
| $f(n) = a^n, \quad a \in \mathbb{R} - \{0\}$   | $(Zf)(z) = \frac{z}{z - a}$  |
| $y(n) = a^n x(n), \quad a \in \mathbb{R} - \{0\}$  | $(Zy)(z) = (Zx)\left(\frac{z}{a}\right)$   |
| $y(n) = x(n - n_0), \quad (n - n_0) \in \mathbb{N}$<br>ou<br>$y(n) = x(n - n_0)e(n - n_0)$ | $(Zy)(z) = z^{-n_0} (Zx)(z)$   |
| $y(n) = x(n + 1)$  | $(Zy)(z) = z [(Zx)(z) - x(0)]$   |
| $y(n) = x(n + 2)$  | $(Zy)(z) = z^2 [(Zx)(z) - x(0) - x(1)z^{-1}]$  |
| $y(n) = x(n + n_0)$  | $(Zy)(z) = z^{n_0} [(Zx)(z) - x(0) - x(1)z^{-1} - x(2)z^{-2} \cdots - x(n_0 - 1)z^{-(n_0 - 1)}]$ |